## Question 1: Rame sec (7 marks)

Give your answer in French, German, Italian or Spanish using a minimum of 30 words.

Aline, Hélène, Zoé, Pierre et Jules veulent traverser une rivière au plus vite. Ils disposent d'une barque ne pouvant contenir que trois personnes au maximum.

Aline et Pierre sont des rameurs expérimentés. Seuls ou à deux, ils peuvent traverser en deux minutes. Malheureusement, les trois autres amis sont tellement maladroits que dès que l'un d'entre eux se trouve à bord, la traversée dure huit minutes.

Combien de temps faudra-t-il au minimum pour que les cinq amis se retrouvent de l'autre côté de la rivière? Expliquer.

Alina, Helene, Zoé, Peter und Julian wollen so schnell wie möglich einen Fluss überqueren. In ihrem Ruderboot ist aber nur für höchstens drei Personen Platz.

Alina und Pierre rudern sehr gut. Alleine oder zu zweit können sie den Fluss in zwei Minuten überqueren. Leider sind die anderen so ungeschickt, dass die Überfahrt acht Minuten dauert, sobald einer von ihnen an Bord ist.

Wie lange dauert es mindestes, bis alle fünf Freunde am anderen Ufer sind?
Erklärt eure Antwort.


Aline, Elena, Zoe, Pietro e Giulio desiderano attraversare un fiume il più velocemente possibile.

Hanno a disposizione una barca che contiene al massimo tre persone.
Aline e Pietro sono dei rematori esperti. Da soli o in due, possono attraversare il fiume in due minuti. Sfortunatamente, gli altri tre amici sono così maldestri che, se uno di loro è a bordo, la traversata dura otto minuti.

Quanto tempo sarà necessario come minimo affinché i cinque amici possano ritrovarsi sull'altra sponda? Spiegate la vostra risposta.

Aline, Elena, Zoe, Pedro y Julio quieren cruzar un río lo más rápido posible. Disponen de una barca que solo puede transportar tres personas como máximo.
Aline y Pedro son remeros experimentados. Solos o con dos, pueden cruzar en dos minutos. Desgraciadamente, les otros tres amigos son tan torpes que desde que uno de ellos se encuentra a bordo, la travesía dura ocho minutos.
¿Cuánto tiempo, como mínimo, hará falta para que los cinco amigos se encuentren al otro lado del río? Explica tu respuesta.

## Question 2: Building blocks (5 marks)

Ravane, Bernard and Jeanne are playing with small cubes of identical size.
Ravane has a small red cube weighing 5 grams.
Bernard surrounds Ravane's cube with small blue cubes, each weighing 8 grams, so that the new structure is also a cube.
Jeanne places small green cubes, each weighing 12 grams, around Bernard's cubes to form a new cube made up of 125 small cubes.
Calculate the total mass of the final cube..


## Question 3: Tak Tent

## (7 marks)

Tula is designing a makeshift tent from a piece of cloth. To do this, she uses her walking sticks each of height 1.2 metres as the tent poles placed vertically at points A and B, which are 1.8 metres apart.
She uses cords, held to the ground by pegs, to keep the tent in place. One cord is placed over both sticks and pegged on either side of the line joining A and B. One peg is 1.5 metres away from A , the other 1.5 metres from B .

Two other pegs are placed along the perpendicular bisector of the line AB , each one 0.9 metres on either side of the midpoint of AB . A cord connects these two pegs to the two tops of the sticks.

Each face of Tula's tent is a triangle.
To complete her design, she needs to cut out the pattern from the cloth.
Draw a net of Tula's pattern, using a scale of 1/30.


## Question 4 : Nursery ( 5 marks)

To grow chicks, a farmer places them in little boxes in a chicken coop. He installs heating lamps in boxes in the coop according to the following rules:

- the box with a lamp has only one side in common with that of the chick's box;
- the heating lamp must be pointed towards the chick's box;
- to avoid overheating, two heating lamps cannot be placed next to each other (including diagonally).
The diagram below shows a plan of the chicken coop. The numbers indicate the number of heating lamps in each row and column. The arrow represents a lamp and the direction in which it is pointing.


Copy and complete the diagram to show the placement of the heating lamps in the chicken coop.

## Question 5: Some Sums (7 marks)

What is the smallest number whose digits add up to 12? Or to 38? Or 2018? Explain your answer.


## Question 6: Curtains! (5 marks)

A youth hostel in the Scottish Highlands has a large dormitory with 15 beds arranged side by side, as shown in the picture below.
The hostel manager regularly hosts hikers who arrive in groups of varying sizes.
He wants to place four curtains, which can be opened or closed, to create all the possible spaces from one to ten beds as needed for the different sizes of group.

## Where should he place the four curtains?




## Question 7: They'll never know (7 marks)

Pierre has been given a Computer-aided design device which can be programmed to draw lines as it moves over a sheet of paper.

The device is given its instructions as:
Go forward .... mm
Turn ..... ${ }^{\circ}$ (the device does not move forward but turns on the spot towards the left)
Repeat ..... times
Some examples include:

- to draw an equilateral triangle of sides 6 cm , you would programme:

Repeat 3 times (Go forward $\mathbf{6 0 m m}$ and then turn through $\mathbf{1 2 0}^{\boldsymbol{\circ}}$ )

- to draw a square of side 6 cm , you would programme:

Repeat 4 times (Go forward 60 mm and then turn through $90^{\circ}$ ).
Pierre wants to draw a circle of radius 10 cm . He thinks that if he draws a regular hectogon, a polygon of 100 sides, then no-one could tell the difference between that and a circle.

Write a programme that Pierre could use to draw the hectogon.


## Question 8: The heart of the matter 5 marks

Four joggers train using their smart watch to constantly measure and display their heart rate. After consulting their watch, they are able to determine the type of exercise they are doing. Here is some information to help them:

- the reserve heart rate (RHR) which is the difference between the maximum heart rate and the rest heart rate;
- each person has his own RHR; and
- the heart rate increases during an exercise session.

| E = difference between measured <br> heart rate and rest heart rate. | Type of exercise |
| :---: | :---: |
| $\mathrm{E}<0.6 \times \mathrm{RHR}$ | Warm up or warm down |
| $0.6 \times \mathrm{RHR} \leq \mathrm{E}<0.7 \times \mathrm{RHR}$ | Basic endurance |
| $0.7 \times \mathrm{RHR} \leq \mathrm{E}<0.8 \times \mathrm{RHR}$ | Active endurance |
| $\mathrm{E} \geq 0.8 \times \mathrm{RHR}$ | Anaerobic activity |


| Name | Rest heart rate | Maximum heart <br> rate | RHR | Measured heart <br> rate |
| :---: | :---: | :---: | :---: | :---: |
| Marc | 60 | 180 | 120 | 108 |
| Luc | 65 | 175 |  | 155 |
| Matthieu | 70 | 170 |  | 135 |
| Jean | 80 | 162 |  | 142 |

Marc's exercise is of the " warm up or wind down " type. Find the type of exercise that Luc, Matthieu and Jean have done. Justify your answers.
]


## Question 9: Price at the pump (7 marks)

A fuel pump display is shown below :

| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | , | $\mathbf{0}$ | $\mathbf{0}$ | $\boldsymbol{€}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | , | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{L}$ |
| $\mathbf{1 , 0 3 2} \mathbf{€} / \mathbf{L}$ |  |  |  |  |  |  |

Draw an example of this display for which the two numbers - volume (in litres) and price (in euros) - differ by exactly 1.
Can this be seen again for other displays?


## Question 10 Whatever (10 marks)

The line OT is 10 cm long.
You have to draw a triangle OPT which looks neither isosceles nor right-angled.
To do that you want to make sure that the vertex $P$ is more than 1 cm away from any of the vertices C where OCT is an isosceles or a right-angled triangle.

Draw the line OT and colour in the area where the point P could be placed.


## Question 11: Right Time (5 marks - senior classes only)

A clock has a long hand to show minutes and short hand to show hours.
Between midday and midnight, how many times do the two hands make a right angle? Explain your answer.


## Question 12: Box clever (7 marks- senior classes only)

A football coach wants to put footballs of diameter 17 cm in a box. The box is a cuboid with base 17 cm by 30 cm and height 1 m .

Find the maximum number of balls that can be put into the box so that the coach can still put on the lid and close the box. Justify your answer.


## Question 13 Astronomical figure (10 marks - senior classes only)

One 14th July Mars, Earth and the Sun were in a straight line. Earth was between Mars and the Sun. 106 days later on the 28th October it was found by observation from Earth that the angle Sun-Earth-Mars was a right angle.

We can simplify by assuming:

- that the Earth goes once round the Sun, in a circle, at constant speed, in 365 days;
- that Mars goes once round the Sun, in a circle, at constant speed, in 687 days;
- the paths taken by Earth and Mars are in the same plane;
- the distance from the Earth to the Sun is about 150 million kilometres.


## Work out a good estimate of the distance of Mars from the Sun.



Note: the diagram shows the Sun, S, and Mars, M. The Earth (la Terre) is shown as $T$.

## Question 13 Boule (10 marks)

## secondes professionnelles classes only

One of the last stages in making a boule for the game of pétanque is to engrave on it the circle pattern. The model shown here has six circles of the same radius engraved on the surface. Each of the circles is a tangent to four other circles. The boule has radius 4 cm .

Draw a front view of this boule on a scale of 1:1. Position your diagram on a set of axes that pass through the centre of an engraved circle and the centre of the boule.

## Find the radius of the circle that needs to be used.

You can use a dynamic geometry software package to answer the question.


Note: The game of pétanque is played with heavy metal boules. The are marked with different circle patterns.

